Mathematical Finance Dylan Possamaï

Recall 4

Itô, Meyer, and Tanaka: formulae

- 1. Can you state the general Itô's formula?
- 2. What is the local time of an (\mathbb{F}, \mathbb{P}) -good integrator X at zero?
- 3. What is the Itô–Tanaka–Meyer formula?

Bichteler–Dellacherie: good integrators are semi-martingales

- 1. Let X be a càdlàg, \mathbb{F} -adapted process. Can you give two equivalent statements to the statement "X is an (\mathbb{F}, \mathbb{P}) -good integrator"?
- 2. Let X be an (\mathbb{F}, \mathbb{P}) -semi-martingale and ξ an \mathbb{F} -predictable process. Can you give an equivalent statement to the statement " $\xi \in \mathcal{L}(X, \mathbb{F}, \mathbb{P})$ "?

Basic notions and probabilistic setting

- 1. What are the five elements that the modern representation and description of a financial market, from a probabilistic perspective, relies on?
- 2. What is a portfolio? When is it said self-financing?
- 3. What is the no-arbitrage condition (NA)?

Abstract financial markets

1. What is the set of m-admissible (\mathbb{F}, \mathbb{P}) -wealth processes?